## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem A : Micromasters

Recently, the Computer Engineering Department has launched its professional education under the title of '"Micromasters", which has been well received by audiences from various universities. Undoubtedly, the quality of these classes played a significant role in this reception. One of the quality factors is to limit the number of registrations for a class. Although the registration for this semester has ended, the director of professional education has decided to limit the number of registrations for each class to 50 and make an urgent decision for the classes with more than 50 students registered. Help the director of professional education to identify which classes have more than 50 students registered.

## Input

The only line of the input consists of $n(1 \leqslant n \leqslant 100)$, the number of registrations in a class.

## Output

In the only line of output, Print Yes if $n>50$, and No otherwise.

## Example

| Standard Input |  | Standard Output |
| :--- | :--- | :--- |
| 45 | No |  |


| Standard Input |  | Standard Output |
| :--- | :--- | :--- |
| 50 | No |  |


| Standard Input | Standard Output |
| :--- | :--- | :--- |
| 78 | Yes |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem B : Sara and Horse

Sara, who is deeply concerned about air pollution, has sold her car and bought a horse. She happily leads the horse to the parking lot and takes a very long string of pasta from the kitchen, which she gives to the horse. The horse happily takes several bites of pasta. Sara's father, who notices the disappearance of the pasta string, finds the remaining pieces of pasta in the parking lot. Being an intelligent person, he knows that the horse selects a piece of pasta longer than 3 inches for each bite. Then, by biting 3 inches from the middle of the selected piece, she divides it into two pieces.

Given the lengths of the remaining pasta pieces, help Sara's father determine the length of the initial pasta string.

## Input

The first line of the input contains an integer $n(1 \leqslant n \leqslant 100)$, which is the the number of remaining pasta pieces. The next line contains a sequence $l_{1}, l_{2}, \ldots, l_{n}$ of $n$ integers, where $l_{i}\left(1 \leqslant l_{i} \leqslant 1000\right)$ represents the length of the $i$ th remaining pasta piece.

## Output

In the only line of output, print the length of the initial pasta string.

|  | Standard Input |  | Standard Output |
| :--- | :--- | :--- | :--- |
| 2 |  | 10 |  |
| 2 | 5 |  |  |


|  | Standard Input |  | Standard Output |
| :--- | :--- | :--- | :--- |
| 2 |  | 18 |  |
| 6 | 9 |  |  |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem C : The Niece

Sara wants to entertain her niece with $n$ coins she has in her pocket. To do this, she arranges a game. In this game, several coins should initially be placed on the table. Then, in each turn, a player must remove either 1 or exactly 4 coins from the table and pass the turn to the other player. The winner is the person who takes the last coin or coins. Sara, due to her love for her niece, allows her niece to start the game. Help Sara determine whether he can definitely win the game by placing all his coins on the table or not.

## Input

The input consists of a single integer $n\left(1 \leqslant n \leqslant 10^{18}\right)$, which represents the number of coins Sara has.

## Output

In the only line of output, print Yes if Sara has a guaranteed winning strategy, and No otherwise.

| Standard Input | Standard Output |
| :--- | :--- | :--- |
| 1 | No |


| Standard Input | Standard Output |  |
| :--- | :--- | :--- |
| 2 | Yes |  |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem D : Binary Majid

Majid has a binary string of length $n$ with only 1 values. One morning, his niece accidentally finds this string and starts destroying it. She destroys the string in $t$ steps. The niece first chooses a sequence of integers: $1 \leqslant a_{1} \leqslant a_{2} \leqslant \ldots \leqslant a_{t} \leqslant n$. Then, in the $i$ th step, she selects the first $a_{i}$ bits and destroys this part as follows:

- First, she negates all the selected bits.
- Then, she reverses the order of the selected part.

To be more precise, if the binary string before the $i$ th step is as follows:

$$
S=s_{1} s_{2}, \ldots, s_{n}
$$

The binary string after the $i$ th step will be as follows, where $\overline{s_{i}}$ represents the negation of bit $s_{i}$ :

$$
S=\bar{s}_{a_{i}}, \bar{s}_{a_{i}-1}, \ldots, \bar{s}_{1}, s_{a_{i}+1}, \ldots, s_{n}
$$

Majid wants to restore the string to its initial state using his superpower. Each time Majid uses his superpower, he chooses two numbers $1 \leqslant l \leqslant r \leqslant n$. Then, magically, all the bits in positions from $l$ to $r$ inclusive are negated. This interval includes the bits at positions $l$ and $r$ themselves. The positions of the bits are considered from left to right, and the leftmost bit has a position of 1 .

Help Majid restore the string to its initial state with the fewest number of uses of his superpower.

## Input

The first line of the input consists of two integers $n\left(1 \leqslant n \leqslant 10^{18}\right)$ and $t\left(1 \leqslant t \leqslant 10^{5}\right)$ separated by a space, which is the length of the string and the number of steps of string destruction, respectively. The second line contains a sequence of integers $a_{1}, a_{2}, \ldots, a_{t}\left(1 \leqslant a_{i} \leqslant n\right)$, chosen by the niece.

## Output

Print $k$, the minimum number of times Majid needs to use his superpower in the first line. Then, in the $(i+1)$ th $(1 \leqslant i \leqslant k)$ line of the output, print the interval that Majid chooses in his $i$ th use of superpower as two numbers separated by a space, in ascending order.

## Example

|  | Standard Input |  | Standard Output |  |
| :--- | :--- | :--- | :--- | :--- |
| 5 | 2 |  | 1 |  |
| 2 | 5 | 1 | 3 |  |


|  | Standard Input |  | Standard Output |
| :--- | :--- | :--- | :--- |
| 5 | 2 |  | 0 |
| 3 | 3 |  |  |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem E : Ants' Movements

A number of ants are located on a two-dimensional plane, and each ant moves either upward or rightward. In each step, each ant moves one unit forward in its direction. More precisely, consider an ant located at coordinates $\left(x_{i}, y_{i}\right)$ before the $i$ th step. If the ant moves upward, its coordinates after the $i$ th step will be $\left(x_{i}, y_{i}+1\right)$, and if it moves rightward, its coordinates after the $i$ th step will be $\left(x_{i}+1, y_{i}\right)$. Initially, no two ants are located at the same coordinates. If two ants collide at the same coordinate in a step, before the next step begins, their movement direction changes from up to right and from right to up. Sara is curious to know the total number of collisions. Given the initial coordinates of the ants and their directions of movement, calculate the total number of collisions for Sara.

## Input

The first line of the input contains an integer $n\left(2 \leqslant n \leqslant 2 \times 10^{5}\right)$, which is the the number of ants. Then, for each $1 \leqslant i \leqslant n$, the $(i+1)$ th line of the input contains two space-separated integers $x_{i}$ and $y_{i}\left(1 \leqslant x_{i}, y_{i} \leqslant 10^{9}\right)$, and one of the letters $U$ or R. The integers denote the initial coordinates of the $i$ th ant, and the letter indicates the initial direction of movement. The letter U represents upward movement, and the letter R represents rightward movement.

## Output

In the only line of output, print the total number of collisions if it is finite, and the word inf otherwise.

|  |  | Standard Input |  |
| :--- | :--- | :--- | :--- |
| 3 |  |  | 1 |
| 1 | 2 | R |  |
| 2 | 1 | U |  |
| 3 | 1 | U |  |


|  |  | Standard Input |  | Standard Output |
| :--- | :--- | :--- | :--- | :--- |
| 4 |  |  | 0 |  |
| 1 | 4 | U |  |  |
| 1 | 2 | U |  |  |
| 1 | 3 | U |  |  |
| 1 | 1 | U |  |  |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem F : Birthday Party

Sara wants to hold a birthday party for her niece. In this ceremony, the guests form a circle around the niece and cheer her up. But the problem is that the heights of the guests present at the birthday party is very different. Therefore, if these guests are randomly placed in the circle, due to the difference in height, they may not be able to hold each other's hands and form the ring. The desired arrangement is a circular arrangement of guests in which the maximum height difference between consecutive individuals is minimum (there may be more than one desired arrangement). For example, if the heights of guests are $3,2,2,4,3,1$, one desired arrangement could be as follows, where the maximum height difference between consecutive individuals is 1 .


By receiving the heights of guests, calculate the maximum height difference between consecutive individuals in a desired arrangement.

## Input

The first line of the input contains an integer $n\left(2 \leqslant n \leqslant 10^{5}\right)$, which is the the number of guests. The next line contains a sequence $l_{1}, l_{2}, \ldots, l_{n}$ of $n$ integers, where $l_{i}\left(1 \leqslant l_{i} \leqslant 10^{9}\right)$ represents the height of the $i$ th guests.

## Output

In the only line of output, print the maximum difference in height between two consecutive individuals in a desired circular arrangement.

|  |  |  |  | Standard Input |  | Standard Output |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 5 |  |  |  |  | 1 |  |  |
| 2 | 1 | 1 | 3 | 2 |  |  |  |


|  | Standard Input |  | Standard Output |  |
| :--- | :--- | :--- | :--- | :--- |
| 3 |  |  | 20 |  |
| 30 | 10 | 20 |  |  |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem G : Arranging Bricks

Majid has $n$ cubic bricks with a unit side length. He wants to arrange these bricks as adjacent columns, such that the height of each column is not less than the height of the previous column. For example, if Majid has two bricks, he can arrange them in two ways. In the first arrangement, he can form a column with a height of 2 , and in the second arrangement, he can create two columns with heights of 1 each. Majid wants to know in how many ways he can do this. Given $n$, calculate the number of possible desired arrangements.

## Input

The input consists of a single integer $n(1 \leqslant n \leqslant 2000)$, which represents the number of bricks Majid has.

## Output

Print a single line containing the number of desired arrangements of the bricks. Since this number can be very large, print its remainder modulo $10^{9}+7$.

| Standard Input |  | Standard Output |
| :--- | :--- | :--- |
| 1 | 1 |  |


| Standard Input | Standard Output |  |
| :--- | :--- | :--- |
| 2 | 2 |  |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem H: Exiting the Matrix

After facing numerous challenges, Majid succeeded in escaping from the matrix. Upon exiting the matrix, he finds himself in an elevator on the $s$ th floor of a building with $f$ floors. Majid quickly realizes that this elevator is not an ordinary one. The elevator has only two buttons: "Up" and "Down". By pressing these buttons, the elevator moves $u$ floors up or $d$ floors down. Specifically:

- After pressing "Up" button, if $c+u \leqslant f$, the elevator goes to floor $c+u$. Otherwise, the elevator remains stationary.
- After pressing "Down" button, if $c-d \geqslant 1$, the elevator goes to floor $c-d$. Otherwise, the elevator remains stationary.

The only way to exit the building is the $g$ th floor. Since exiting the elevator shouldn't be easy, each time Majid presses either the "Up" or "Down" button, he has to pay a high cost. Shocked by the conditions, Majid asks you to calculate the minimum cost for him to exit the building.

## Input

In the only input line, you are given integers $f, s, g, u$, and $d$ separated by a space from left to right $(1 \leqslant s, g \leqslant f \leqslant$ $10^{6}, \quad 0 \leqslant u, d \leqslant 10^{6}$ ).

## Output

In the only line of output, print the minimum number of times Majid needs to press the elevator buttons to exit the building. If it is impossible to reach from floor $s$ to floor $g$ using the elevator, print use the stairs.

|  | Standard Input |  | Standard Output |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 10 | 1 | 10 | 2 | 1 | 6 |  |


| Standard Input |  |  |  | Standard Output |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 100 | 2 | 1 | 0 | use the stairs |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024

## Problem I: Planting Flowers

As spring arrives, Majid plans to beautify his backyard by planting flowers. To achieve this, he has divided his backyard into an $m \times n$ grid and has decided to plant red or blue roses in each cell. Majid has a keen eye for colour combinations and wants to ensure that each cells has at most one neighboring cell of the same color. Two cells are considered adjacent if they share at least one side. Given $m$ and $n$, calculate the number of desired ways to arrange the flowers in the grid for Majid. For example, if the dimensions of the grid are $2 \times 3$, there are 8 possible ways to arrange the flowers in the grid as shown below:


## Input

The first line of the input consists of two integers $m\left(1 \leqslant m \leqslant 10^{5}\right)$ and $n\left(1 \leqslant n \leqslant 10^{5}\right)$ separated by a space, which is the number of rows and the number of columns, respectively.

## Output

Print a single line containing the number of desired ways to plant the flowers. Since this number can be very large, print its remainder modulo $10^{9}+7$.

| Standard Input |  | Standard Output |
| :--- | :--- | :--- |
| 23 | 8 |  |


|  | Standard Input |  | Standard Output |
| :--- | :--- | :--- | :--- |
| 12 | 4 |  |  |

## 20th Iran Internet Programming Contest

Asia Region, Tehran Site, Qualification Round
Sharif University of Technology, 1 May 2024


## Problem J : Travel

The subway system in Barareh consists of $n$ stations and $m$ subway lines. The stations are numbered from 1 to $n$. Each line is managed by a company and each company has a unique identifier. The $i$-th subway line ( $1 \leqslant i \leqslant m$ ) is managed by company $c_{i}$ and connects only two stations, $p_{i}$ and $q_{i}$, in both directions. When arriving at a station, if more than one subway line is connected to that station, passengers can easily switch between lines.

The cost of using the subway in Barareh is a bit different. When a passenger uses only subway lines operated by a single company, he only need to pay 1 Bararehian dollar. However, if a passenger changes their subway line at a station, and these two lines are managed by different companies, he have to pay an additional 1 Bararehian dollar. In other words, the passenger pays 1 Bararehian dollar at the first station, and then at each intermediate station, they only need to pay an additional 1 Bararehian dollar if the two lines used for arriving and departing the station belong to different companies. Calculate the minimum cost required to travel from station 1 to station $n$.

## Input

The first line of the input consists of two integers $n\left(2 \leqslant n \leqslant 10^{5}\right)$ and $m\left(0 \leqslant m \leqslant 2 \times 10^{5}\right)$ separated by a space, which is the number of stations and the number of subway lines, respectively. Then, for each $1 \leqslant i \leqslant m$, the $(i+1)$-th line of input contains three integers $p_{i}, q_{i}$, and $c_{i}\left(1 \leqslant c_{i} \leqslant 10^{6}\right)$, separated by a space ( $p_{i} \neq q_{i}, \quad 1 \leqslant p_{i}, q_{i} \leqslant n$ ).

## Output

In the only line of output, if it is impossible to travel from station 1 to station $n$ using the subway lines, print -1 . Otherwise, print the minimum cost required to travel from station 1 to station $n$.

|  | Standard Input |  | Standard Output |
| :--- | :--- | :--- | :--- |
| 3 | 3 |  | 1 |
| 1 | 2 | 1 |  |
| 2 | 3 | 1 |  |
| 3 | 1 | 2 |  |


|  | Standard Input |  |  |
| :--- | :--- | :--- | :--- |
| 8 | 11 |  | Standard Output |
| 1 | 3 | 1 |  |
| 1 | 4 | 2 |  |
| 2 | 3 | 1 |  |
| 2 | 5 | 1 |  |
| 3 | 4 | 3 |  |
| 3 | 6 | 3 |  |
| 3 | 7 | 3 |  |
| 4 | 8 | 4 |  |
| 5 | 6 | 1 |  |
| 6 | 7 | 5 |  |
| 7 | 8 | 5 |  |

In the example above, initially, one can traverse the following path by paying 1 Bararehian dollar: $1 \rightarrow 3 \rightarrow 2 \rightarrow 5 \rightarrow 6$ Then, with another 1 Bararehian dollar payment, continue the path as follows: $6 \rightarrow 7 \rightarrow 8$.

